

## COTAS ASINTÓTICAS MÁS USUALES

1.  $c \in \Theta(1), \forall c \in \mathbb{R}^{\geq 0}$
2.  $\sum_{i=1}^n i = n/2 (n+1) \in \Theta(n^2)$
3.  $\sum_{i=1}^n i^2 = n/3 (n+1)(n+1/2) \in \Theta(n^3)$
4.  $\sum_{i=1}^n i^k \in \Theta(n^{k+1}), \forall k \in \mathbb{N}$
5.  $\sum_{i=1}^n (n-i)^k \in \Theta(n^{k+1}), \forall k \in \mathbb{N}$
6.  $\sum_{i=1}^n r^i = (r^{n+1}-1)/(r-1) \in \Theta(r^n), r \neq 1$
7.  $\sum_{i=1}^n 1/i = H_n = \ln n + \gamma + O(1/n) \in \Theta(\lg n)$  (serie harmónica)
8.  $\sum_{i=1}^n (1/r^i) \in \Theta(1)$  si  $r > 1$
9.  $\sum_{i=0}^{n-1} H_i = n H_n - n \in \Theta(n \lg n)$
10.  $\sum_{i=1}^n i H_i = n/2 (n+1) H_{n+1} - n/4 (n+1) \in \Theta(n^2 \lg n)$
11.  $\sum_{i=1}^n \lg i \in \Theta(n \lg n)$
12.  $\sum_{i=1}^n i 2^{i-1} = n2^n - 2^n + 1 \in \Theta(n2^n)$
13.  $\sum_{i=1}^n i 2^{-i} = 2 - n/2^n - 2/2^n \in \Theta(1)$
14.  $\sum_{i=1}^n i r^{i-1} \in \Theta(nr^n), \forall r > 1$
15.  $\sum_{i=1}^n i r^i \in \Theta(1), \forall r > 1$
16.  $\sum_{i=1}^n 1/i! \in \Theta(1)$
17.  $\sum_{i=1}^n \binom{n}{i} = 2^n \in \Theta(2^n)$
18.  $n! = \sqrt{2\pi n} \left(\frac{n}{e}\right)^n \left(1 + \Theta\left(\frac{1}{n}\right)\right) \in \Theta\left(\sqrt{n} \left(\frac{n}{e}\right)^n\right)$